

# Local Linearizability

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# Concurrent Data Structures

## Correctness and Performance

# Semantics of concurrent data structures

t1: enq(2) deq(1)  
t2: enq(1) deq(2)

e.g. pools, queues, stacks

- Sequential specification = set of legal sequences

e.g. queue legal sequence  
enq(1)enq(2)deq(1)deq(2)

- Consistency condition = e.g. linearizability / sequential consistency

e.g. the concurrent history above is a linearizable queue concurrent history

# Consistency conditions

there exists a legal sequence that preserves precedence

Linearizability [Herlihy, Wing '90]

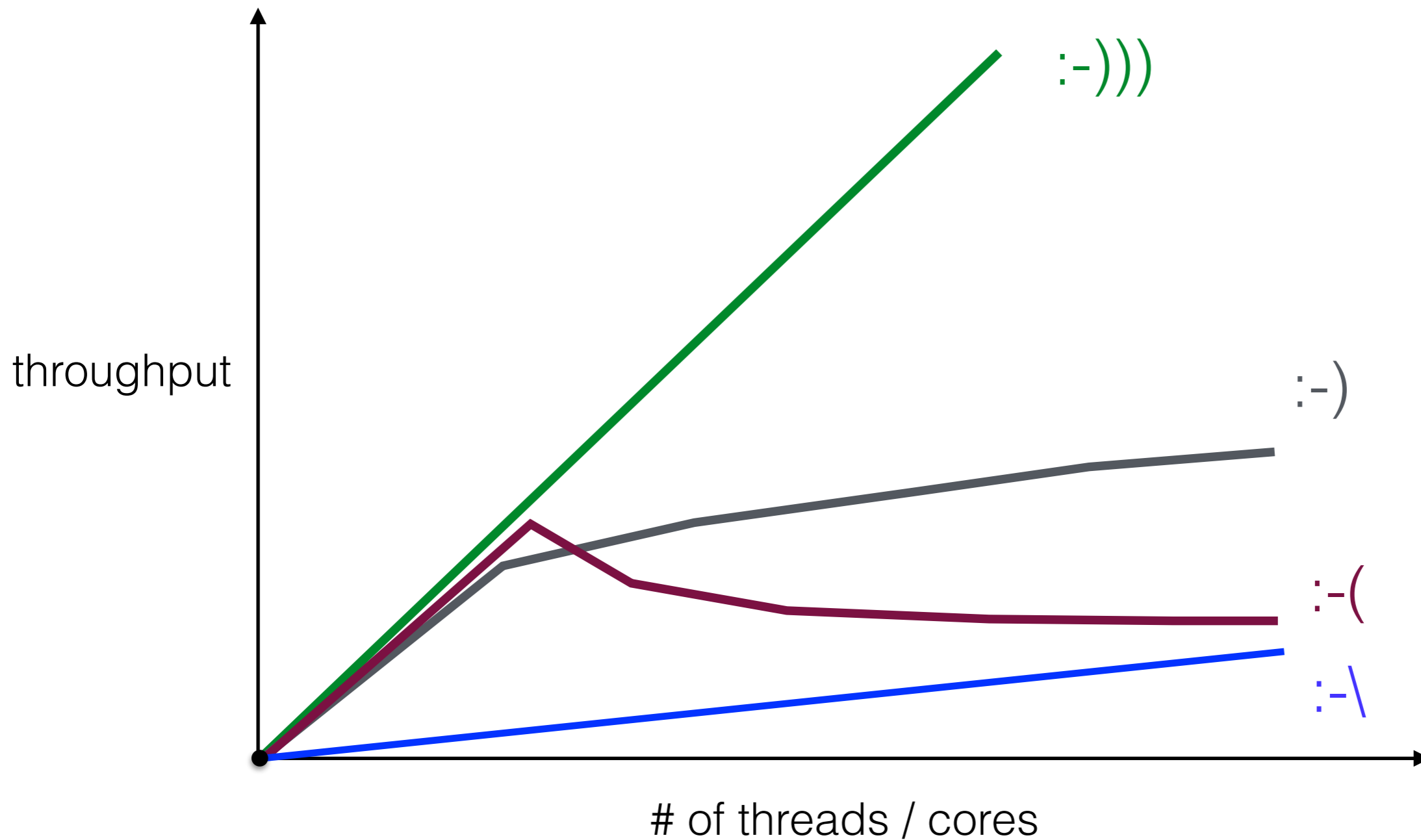
t1: enq(2)<sup>2</sup> — deq(1)<sup>3</sup>  
t2: <sup>1</sup>enq(1) — deq(2)<sup>4</sup>

Sequential Consistency [Lamport'79]

there exists a legal sequence that preserves per-thread precedence (program order)

t1: <sup>1</sup>enq(1) — deq(2)<sup>4</sup>  
t2: deq(1)<sup>2</sup> — enq(2)<sup>3</sup>

# Performance and scalability



# Relaxations allow trading

correctness  
for  
performance

provide the **potential**  
for better-performing  
implementations

# Relaxing the Semantics

not  
“sequentially  
correct”

Quantitative relaxations - POPL13  
Henzinger, Kirsch, Payer, Sezgin, S.

- Sequential specification = set of legal sequences
- Consistency condition = e.g. linearizability / sequential consistency

for queues only  
(feel free to ask for more)

Local linearizability - CONCUR16  
in this talk

too weak



# Local Linearizability

## main idea

Already present in some shared-memory consistency conditions  
(not in our form of choice)

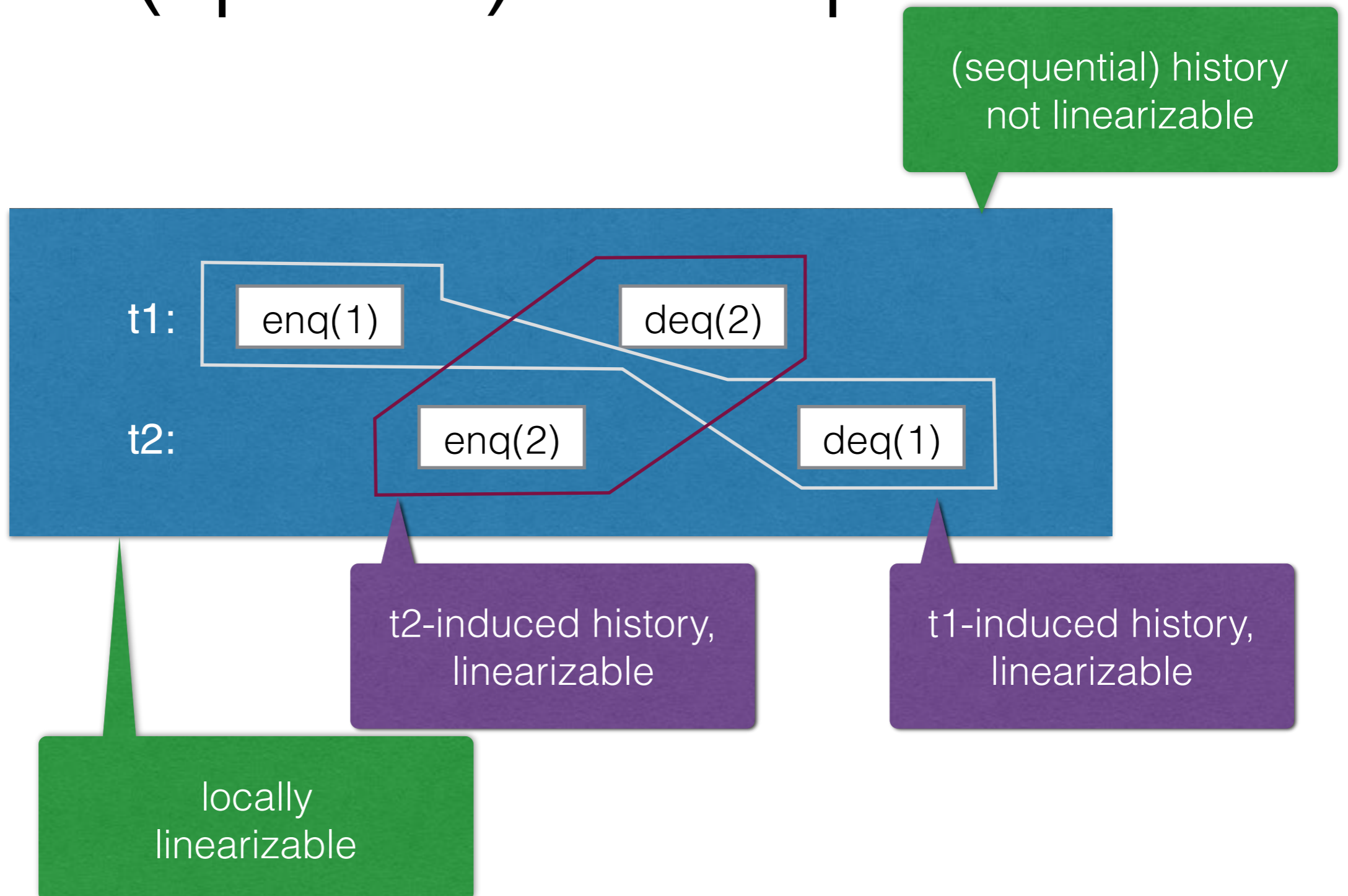
- **Partition** a history into a set of local histories
- Require **linearizability per local history**

no global witness

Local sequential consistency... is also possible



# Local Linearizability (queue) example



# Local Linearizability (queue) definition

Queue signature  $\Sigma = \{\text{enq}(x) \mid x \in V\} \cup \{\text{deq}(x) \mid x \in V\} \cup \{\text{deq}(\text{empty})\}$

For a history  $\mathbf{h}$  with a thread  $T$ , we put

$$I_T = \{\text{enq}(x)^T \in \mathbf{h} \mid x \in V\}$$

$$O_T = \{\text{deq}(x)^T \in \mathbf{h} \mid \text{enq}(x)^T \in I_T\} \cup \{\text{deq}(\text{empty})\}$$

in-methods of thread  $T$   
are  
enqueuees performed  
by thread  $T$

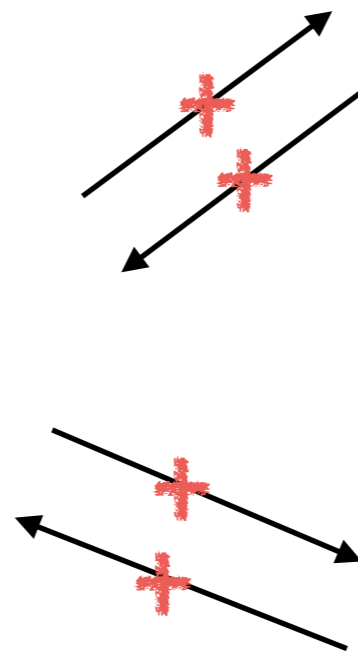
out-methods of thread  $T$   
are dequeuees  
(performed by any thread)  
corresponding to enqueuees that  
are in-methods

$\mathbf{h}$  is locally linearizable iff every thread-induced history  
 $\mathbf{h}_T = \mathbf{h} \mid (I_T \cup O_T)$   
is linearizable.

# Where do we stand?

In general

Local Linearizability



Linearizability

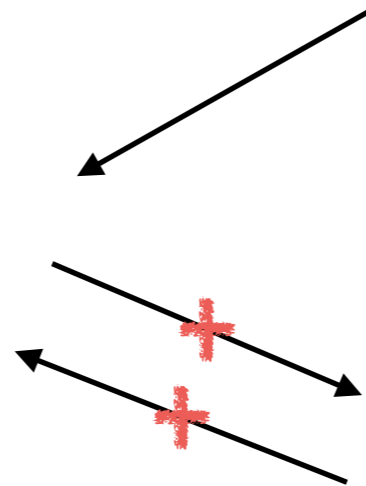


Sequential Consistency

# Where do we stand?

For queues (and most container-type data structures)

Local Linearizability



Linearizability



Sequential Consistency

# Properties

Local linearizability is compositional

like linearizability  
unlike sequential consistency

$h$  (over multiple objects) is locally linearizable  
iff  
each per-object subhistory of  $h$  is locally linearizable

Local linearizability is modular /  
“decompositional”

uses decomposition into smaller  
histories, by definition

may allow for modular verification



# Generic Implementations

Your favorite linearizable data structure implementation

$\Phi$

turns into a locally linearizable implementation by:

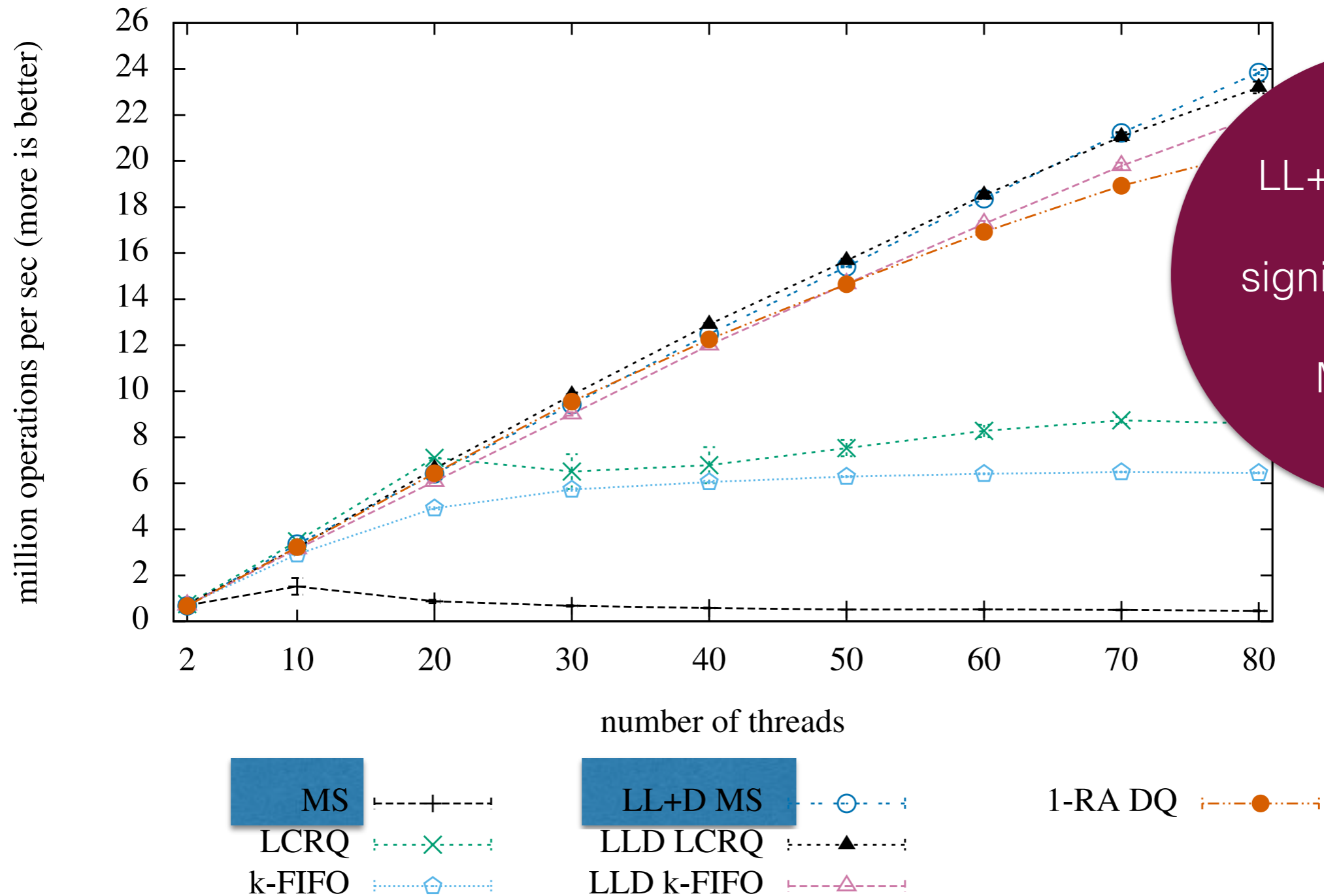
segment of possibly dynamic size (n)

LLD  $\Phi$   
(locally linearizable)

LL+D  $\Phi$   
(also pool linearizable)

local inserts / global (randomly distributed) removes

# Performance

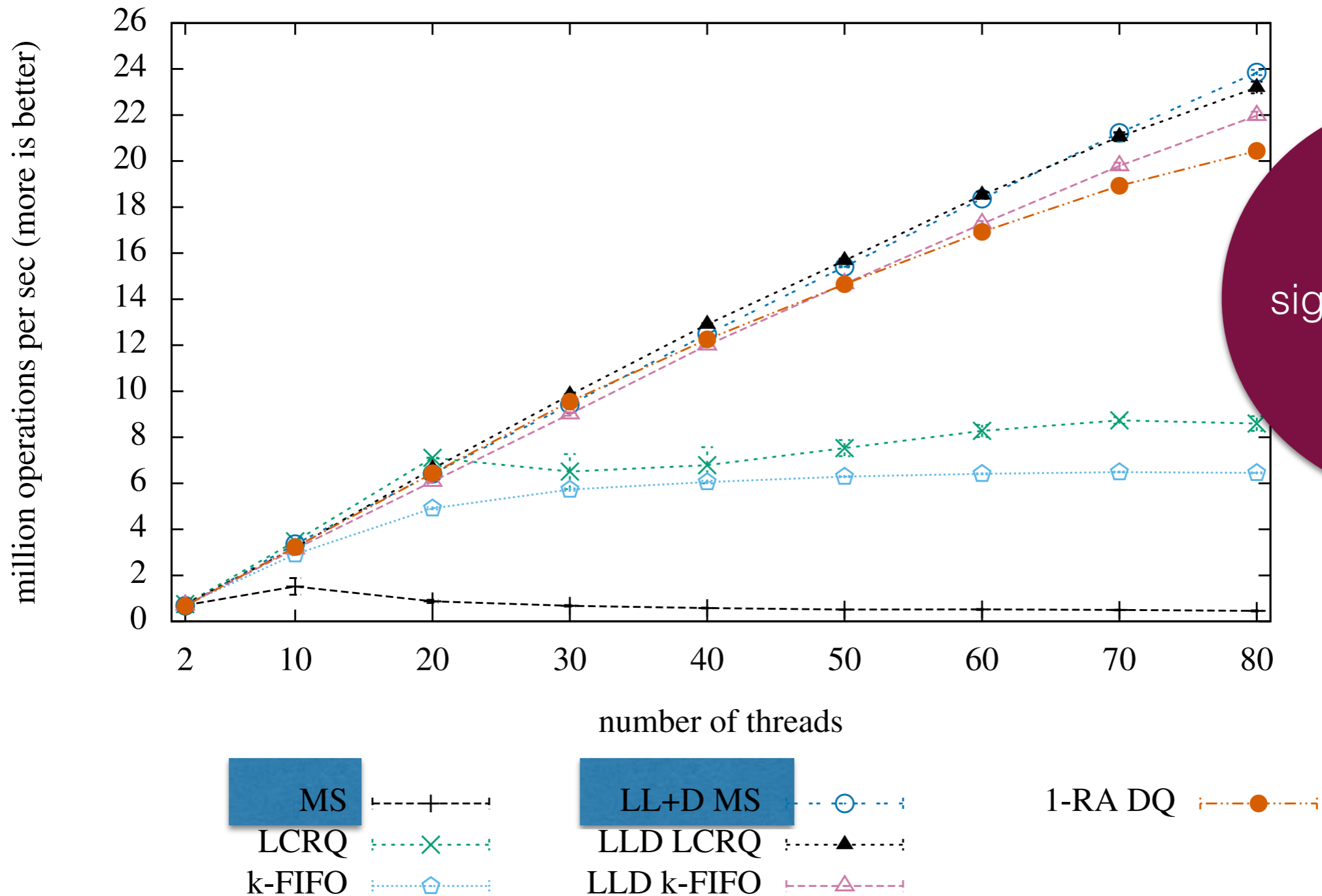


LL+D MS queue performs significantly better than MS queue

(a) Queues, LL queues, and “queue-like” pools



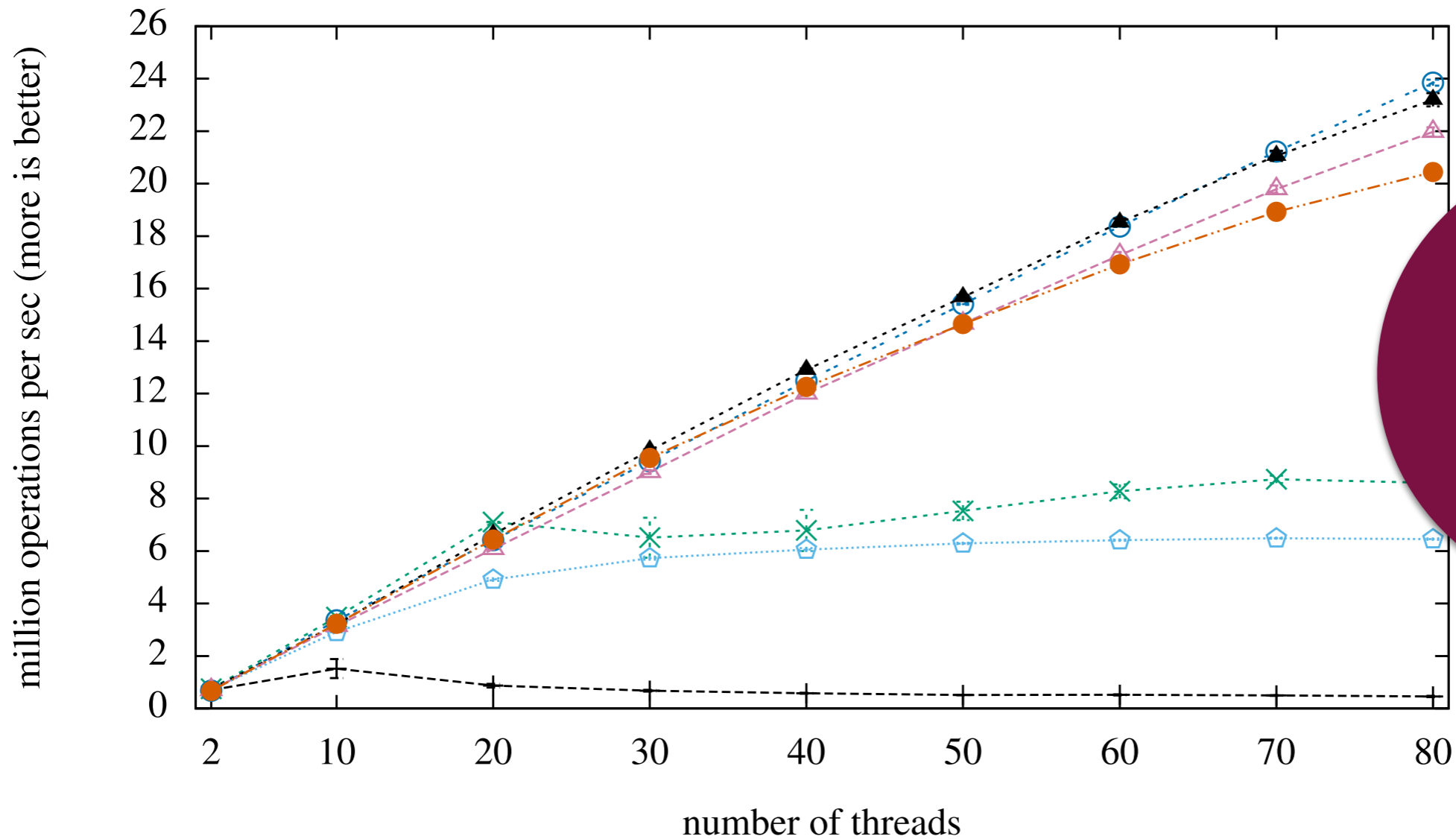
# Performance



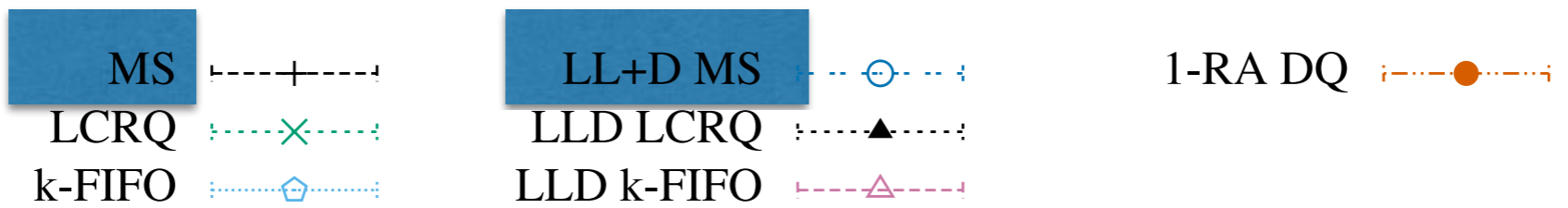
LLD  $\phi$  performs significantly better than  $\phi$

(a) Queues, LL queues, and “queue-like” pools

# Performance



LL+D MS queue performs better than the best known pools



(a) Queues, LL queues, and “queue-like” pools

Thank You!

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